

Comment II on “Possible experiment to check the reality of a nonequilibrium temperature”

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Recently, Jou and Casas-Vázquez [Phys. Rev. A 45, 8371 (1992)] proposed an experiment aimed to verify the physical reality of the nonequilibrium temperature Θ they introduced in their earlier works. I argue here—completely within the framework and philosophy of their theory—that this experiment cannot yield the desired result.

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To investigate the physical reality of the nonequilibrium temperature Θ introduced in their earlier works, Jou and Casas-Vázquez [1] suggest checking whether there arises a heat flux q_x between two connected thermodynamic systems (Fig. 1): The system on the left is in equilibrium, at the temperature T . To the system on the right, the steady heat flux q_y is applied; at the connection point, the local-equilibrium temperature T shall equal the temperature of the equilibrium system.

The theory of Jou and Casas-Vázquez gives for the nonequilibrium temperature Θ

$$\frac{1}{\Theta} = \frac{1}{T} - \gamma \mathbf{q} \cdot \mathbf{q} \tag{1}$$

(cf. Ref. [1] for the definition of γ). It follows also from their theory that a heat flux is driven by a gradient in Θ rather than in T [Eq. (3) of Ref. [1]]. Hence, in the experiment, with T adjusted, the heat flux q_x will arise in the connecting link:

$$q_x = \lambda \frac{T - \Theta}{L}, \tag{2}$$

where λ is the thermal conductivity of the link, and L is its length.

The existence of the heat flux q_x shall, according to Jou and Casas-Vázquez, be interpreted as evidence for the physical reality of the nonequilibrium temperature Θ .

For this experiment to work, it is obviously crucial to prepare the system such that, at the connection point in the nonequilibrium system, T (and not Θ) is equal to T in the equilibrium system. Note that the local-equilibrium temperature T cannot be checked *in situ*: Again within the framework of the theory of Jou and Casas-Vázquez, a thermometer measures Θ , not T . So all depends on the appropriate preparation of the system.

This is done, of course, via an adjustment of the temperatures T'' , T' in the two reservoirs (cf. Fig. 1). The temperature difference ($T'' - T'$) then gives rise to a heat flux in the y direction. Assuming a linear temperature distribution, we simply have

$$q_y = \lambda^* \frac{T'' - T'}{D}. \tag{3}$$

Here, λ^* is the effective heat conductivity of the non-

equilibrium system, and D is its length in the y direction.

One is tempted to conclude that, at the connection point (put in the middle),

$$T = \frac{1}{2}(T'' - T') \tag{4}$$

with $\frac{1}{2}(T'' - T')$ set equal to the temperature in the equilibrium system.

However, this conclusion stands in contradiction to the theory of Jou and Casas-Vázquez: Since the heat flux is driven by the gradient in Θ rather than in T , one expects Θ rather than T to be the temperature that has a linear distribution. This observation results in

$$\Theta = \frac{1}{2}(T'' - T') \tag{5}$$

at the connection point. Hence, if the preparation is such that $\frac{1}{2}(T'' - T')$ equals the temperature in the equilibrium system, then there will not be a Θ gradient in the link, and there will not arise a heat flux q_x .

Actually, $\frac{1}{2}(T'' - T')$ is not too well defined, either. Let us examine the reservoirs a little closer. A thermal reservoir is characterized by an infinite heat capacity C , guaranteeing the constancy of the temperature in time. Now, in the experiment, the reservoirs sustain the heat flux q_y , driven by temperature gradients, and are therefore not in equilibrium. So, in principle, all ambiguities associated with the definition of a temperature in a non-equilibrium system apply to T'' , T' as well.

But fortunately, the coefficient γ is proportional to $1/C$ so that, for a thermal reservoir, $T = \Theta$. The difference between T and Θ starts, and ends, at the reservoir walls: From Eq. (2) of Ref. [1] follows

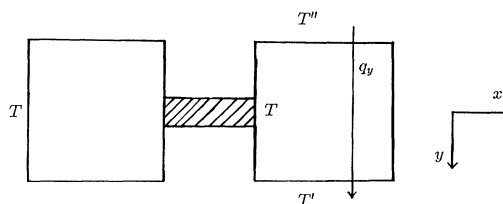


FIG. 1. Experiment proposed by Jou and Casas-Vázquez. The left system is in equilibrium, at the temperature T . The right system is exposed to the steady heat flux q_y . The two systems are connected by a good thermal link.

$$\mathbf{F} = \frac{\mathbf{q}}{\Theta}, \quad (6)$$

where \mathbf{F} is the entropy flux. With no other dissipative processes present, and without the consideration of surface entropy production, \mathbf{F} as well as \mathbf{q} are continuous at the interfaces. This leads to the boundary condition

$$\Theta^{[1]} = \Theta^{[2]}. \quad (7)$$

The local-equilibrium temperature T , on the other hand, generally is *not* continuous [cf. Eq. (1): γ is material-specific]. Hence, if one connects one thermodynamic system to another, better known, one applies the value of Θ to the system, rather than the value of T (Fig. 2).

So, obviously, if the theory of Jou and Casas-Vázquez is correct, their experiment in the suggested form (Ref. [1]) cannot work. If their theory is not correct, their experiment cannot work either: Quite generally, that temperature whose gradient drives the heat flux is also continuous at interfaces, and is such the *only* temperature accessible by thermometry.

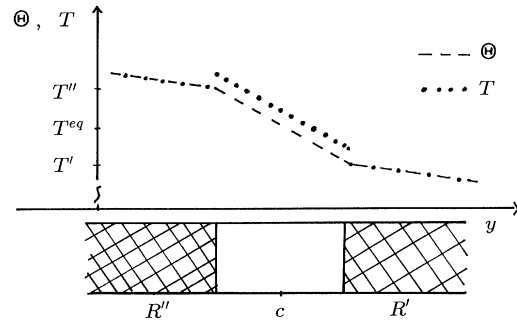


FIG. 2. Slope of the temperatures Θ and T in the nonequilibrium system. R'' , R' are the reservoirs. c is the connection point to the equilibrium system that has the temperature $T = T^{eq}$.

Physical reality can be attributed to more than one temperature only if, for these temperatures, additional equations are available that are independently measurable.

[1] D. Jou and J. Casas-Vázquez, Phys. Rev. A **45**, 8371 (1992).